

# *Techniques for stellar parameter determination*

#### **BETWEEN THE LINES** A Stellar Spectroscopy Workshop

https://www.astronomersdoitinthedark.com/index.php?c=152&p=427

- Chris Sneden
- Department of Astronomy & McDonald Observatory
	- University of Texas at Austin eden

### the overall goal is to extract reliable abundances from observed spectra



https://web.njit.edu/~gary

#### or by extracting the contributions of individual elements in complex blended spectra





which can be interpreted in terms of stellar nucleosynthesis



https://apod.nasa.gov/apod/ap010530.html

### comprehensive texts

Thorough, detailed, mathematical from a theoretical modeling point of view

Ivan Hubeny & Dimitri Mihalas

## **THEORY OF STELLAR ATMOSPHERES**

An Introduction to Astrophysical Non-equilibrium Quantitative Spectroscopic Analysis

SERIES IN ASTROPHYSICS

pragmatic, easily applicable, from an observer's point of view; excellent figures

## The Observation and Analysis of **STELLAR PHOTOSPHERES**

**DAVID F. GRAY** 

**FOURTH EDITION** 

### *minimum* requirements for a spectroscopic analysis

- $\triangleright$  line analysis code for EWs or synthetic spectra
- > stellar model atmosphere ( $\tau$ , T, P<sub>g</sub>, P<sub>e</sub>, (turbulent velocities, ...)
- $\triangleright$  line list ( $\lambda$ , species,  $\chi_{\text{lower}}$  or EP<sub>lower</sub>, gf, (damping, EW, ...)
- $\triangleright$  observed spectrum for EW measurements or syntheses
- my discussion of course will be based on my own code MOOG (Sneden 1973)
- MOOG has its particular assets and liabilities
- but so do all line analysis codes
- your job is to first understand the peculiarities of the code that you adopt/write
- and then to stay in command of what you do
- it is a poor user who blames the code! If a code has unhappy limits, find another code

 $=$   $[X/Y] = log_{10}(N_X/N_Y)_{star} - log_{10}(N_X/N_Y)_{sun}$ 

where N is an elemental number density;

These are abundances relative to the Sun

**•**  $A = \log \varepsilon(X) = \log_{10}(N_X/N_H) + 12.0$  (spectroscopy)

these are "absolute" without reference to the Sun

- $log N(X) = log_{10}(N_X/N_{Si}) + 6.0$  (meteorites)
- Metallicity  $\rightarrow$  [Fe/H]  $\rightarrow$  sometimes labeled [M/H]
- Most metal-rich?  $[Fe/H] \approx +0.5$  (proven)
- Most metal-poor?  $[Fe/H] < \sim -8$  (probably not the limit)
- Metallicity labels (watch out! these vary greatly from paper to paper) **metal-poor: [Fe/H] ≤ -2 very metal-poor: [Fe/H] ≤ -2 extremely metal-poor: [Fe/H] ≤ -3 NATURE paper metal-poor: [Fe/H] ≤ -6 or -7 or …**

## **WATCH OUT! [X/Y] quantities have ASSUMPTIONS**

#### This is the only careful treatment that has been published

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https://doi.org/10.3847/1538-3881/ac9bfa



#### A Concise Treatise on Converting Stellar Mass Fractions to Abundances to Molar Ratios

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#### **Abstract**

Understanding stellar composition is fundamental not only to our comprehension of the Galaxy, especially chemical evolution, but it can also shed light on the interior structure and mineralogy of exoplanets, which are formed from the same material as their host stars. Unfortunately, the underlying mathematics describing stellar mass fractions and stellar elemental abundances is difficult to parse, is fragmented across the literature, and contains vexing omissions that makes any calculation far from trivial, especially for nonexperts. In this treatise, we present a clear mathematical formalism and clarification of inherent assumptions and normalizations within stellar composition measurements, which facilitates the conversion from stellar mass fractions to elemental abundances to molar ratios, including error propagation. We also provide an example case study of HIP 544 to further illustrate the provided equations. Given the important chemical association between stars, as well as the interdisciplinary relationship between stars and their planets, it is vital that stellar mass fractions and abundance data be more transparent and accessible to people within different subfields and scientific disciplines.

## stellar line formation

there are many good sources, especially in texts by Hubeny & Milahas (2014), Gray (2021), LeBlanc (2010), Crivellari et al. (2012)

all discuss the pathways from:

$$
\mu \frac{\mathrm{d}I_{\nu}}{\mathrm{d}\tau_{\nu}} = I_{\nu} - S_{\nu}.
$$

$$
\text{to:} \qquad \qquad I_{\nu}^{+}(0,\mu) \;\; = \;\; \int_{0}^{\infty} S_{\nu}(\tau_{\nu}) \; \mathrm{e}^{-\tau_{\nu}/\mu} \; \mathrm{d}\tau_{\nu}/\mu
$$
\n
$$
\mathcal{F}_{\nu}^{+}(0) \;\; = \;\; 2\pi \int_{0}^{\infty} S_{\nu}(\tau_{\nu}) \, E_{2}(\tau_{\nu}) \; \mathrm{d}\tau_{\nu}
$$

using quantities that you might be able to measure:

$$
\left[\alpha_{\nu}^{l}\right]_{\text{LTE}} = \frac{\pi e^2}{m_e c} n_l^{\text{LTE}} f_{l\mu} \varphi(\nu - \nu_0) \left[1 - e^{-h\nu_0/kT}\right]
$$

## line analysis codes: a partial list of popular ones

#### Line analysis code:

- Kurucz WIDTH: [http://kurucz.harvard.edu/programs/WIDTH](http://kurucz.harvard.edu/programs/WIDTH/)
- Kurucz SYNTHE: [http://kurucz.harvard.edu/programs/SYNTHE](http://kurucz.harvard.edu/programs/SYNTHE/)
- **E** Hubeny TLUSTY: [http://nova.astro.umd.edu](http://nova.astro.umd.edu/)
- Plez TURBOSPECTRUM: [http://www.pages-perso-bertrand-plez.univ-montp2.fr](http://www.pages-perso-bertrand-plez.univ-montp2.fr/)
- Masseron BACCHUS: <https://ui.adsabs.harvard.edu/abs/2016ascl.soft05004M/abstract>
- Sneden MOOG: <http://www.as.utexas.edu/~chris/moog.html>
- **E** Wheeler KORG: <https://github.com/ajwheeler/Korg.jl>
- Other personal programs not generally available to public

#### WHICH CODE TO USE? *WHO CARES!* KEEP FOCUSED ON WHAT YOU WANT AND BE HONEST ABOUT WHAT YOU REPORT

These codes all have tradeoffs between convenience, speed, and sophistication of basic physics:

- **EXECUTE:** Allowance for scattering in continuum opacities & source functions
- **E** LTE or "better"
- How much atomic/molecular information comes with code
- Plane-parallel or spherical geometry
- **<u>■ User friendliness</u>**
- Common-sense outputs that help user avoid stupidities

## MOOG was written to try to mimic Edmonds (1969)

J. Quant. Spectrosc. Radiat. Transfer. Vol. 9, pp. 1427-1446.

#### RADIATIVE TRANSFER WITHIN A STELLAR ABSORPTION LINE. THE CONTRIBUTION CURVES OF FINE-ANALYSIS METHODS

FRANK N. EDMONDS, JR.

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local thermodynamic equilibrium (LTE), plain-parallel geometry, no spots, magnetic fields, simple microturbulence description, ...

Don't be a coward! It is simple FORTRAN coding meant to be available for modification by users, so look "under the hood" to find where these equations live:

This is a good paper to understand "contribution curves"

$$
D(\Delta \lambda) = \int_{-\infty}^{\infty} C_D(\Delta \lambda, x) dx.
$$
 (13)

When pure absorption or equation (4) is assumed, equations  $(1)$ –(3) and  $(5)$ –(7) give

$$
C_R(\Delta \lambda, x) = \frac{2\tau(x)}{0.4343 F_\lambda(0)} \frac{\varkappa_\lambda(x)}{\varkappa(x)} B_\lambda(T[x]) \left\{ 1 + \frac{\varkappa_\nu(x)}{\varkappa_\lambda(x)} E_2(\tau_\lambda[x] + \tau_\nu[x]), \right\}
$$
(14)

where  $x(x)$  is the opacity associated with the reference optical depth;

$$
C_D(\Delta \lambda, x) = \frac{2\tau(x)}{0.4343 F_\lambda(0)} \frac{\varkappa_\lambda(x)}{\varkappa(x)} B_\lambda(T[x])
$$

$$
\times \left[ E_2(\tau_\lambda[x]) - \left\{ 1 + \frac{\varkappa_\nu(x)}{\varkappa_\lambda(x)} \right\} E_2(\tau_\lambda[x] + \tau_\nu[x]) \right]
$$

$$
= \frac{C_\lambda(x)}{F_\lambda(0)} - C_R(\Delta \lambda, x) \tag{15}
$$

for the F-S method, where  $C_1(x)$  is the continuum contribution curve at the wavelength of the line;

$$
C_D(\Delta \lambda, x) = \frac{2}{F_{\lambda}(0)} \frac{dB_{\lambda}(T[x])}{dx} [E_3(\tau_{\lambda}[x]) - E_3(\tau_{\lambda}[x] + \tau_{\nu}[x])]
$$
(16)

for the P-G method; and

$$
C_D(\Delta \lambda, x) = \frac{2\tau(x)}{0.4343 F_\lambda(0)} \frac{\varkappa_v(x)}{\varkappa(x)} \int\limits_{-\infty}^{\infty} \frac{\mathrm{d}B_\lambda(T[x'])}{\mathrm{d}x'} E_2(\tau_\lambda[x'] + \tau_v[x]) \,\mathrm{d}x' \tag{17}
$$

for the W-S method.

and

In these equations,

$$
\tau_{\nu}(x) = \frac{1}{0.4343} \int_{-\infty}^{x} \tau(x') \frac{\varkappa_{\nu}(x')}{\varkappa(x')} dx',
$$
\n(18)

$$
\varkappa_{\nu}(x) = N(x) \frac{\pi e^2}{mc} \frac{f}{\Delta \nu_D(x)} [1 - e^{-hc/\lambda k T(x)}] U(a[x], v[x]), \tag{19}
$$

$$
\Delta v_D(x) = \frac{1}{\lambda} \left[ \frac{2kT(x)}{M} + \xi^2(x) \right]^{1/2},\tag{20}
$$

$$
v(x) = \Delta \lambda \bigg/ \frac{\lambda}{c} \bigg[ \frac{2kT(x)}{M} + \xi^2(x) \bigg]^{1/2}, \tag{21}
$$

 $(22)$ 

#### *Requirement for chemical composition analyses:*

#### A grid of model stellar photospheres:

- Kurucz ATLAS: <http://kurucz.harvard.edu/grids.html>
- Gustafsson MARCS: [http://marcs.astro.uu.se](http://marcs.astro.uu.se/)
- Hauschildt PHOENIX: <https://www.physik.uni-hamburg.de/en/hs/group---hauschildt.html>

#### Typical model atmosphere output: Kurucz ATLAS

TEFF 3500. GRAVITY 0.00000 LTE TITLE SDSC GRID [+0.0] VTURB 0.0 KM/S L/H 1.25 OPACITY IFOP 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 0 0 0 0 0 CONVECTION ON 1.25 TURBULENCE OFF 0.00 0.00 0.00 0.00 ABUNDANCE SCALE 1.00000 ABUNDANCE CHANGE 1 0.91100 2 0.08900 READ DECK6 72 RHOX,T,P,XNE,ABROSS,ACCRAD,VTURB 1.92081317E-02 2162.9 1.918E-02 3.953E+05 6.942E-06 1.304E-03 0.000E+00 2.55242080E-02 2185.4 2.549E-02 5.259E+05 7.141E-06 1.219E-03 0.000E+00 3.37376143E-02 2204.8 3.370E-02 6.928E+05 7.301E-06 1.118E-03 0.000E+00 4.44603299E-02 2223.3 4.441E-02 9.084E+05 7.451E-06 1.024E-03 0.000E+00 5.84449198E-02 2243.2 5.838E-02 1.191E+06 7.631E-06 9.457E-04 0.000E+00 7.66163984E-02 2264.8 7.653E-02 1.561E+06 7.847E-06 8.769E-04 0.000E+00 1.00122149E-01 2288.2 1.000E-01 2.047E+06 8.106E-06 8.122E-04 0.000E+00 1.30562972E-01 2308.0 1.304E-01 2.662E+06 8.320E-06 7.329E-04 0.000E+00 1.70060206E-01 2328.6 1.699E-01 3.462E+06 8.564E-06 6.653E-04 0.000E+00 construction of model atmospheres is a long subject for textbooks

 $R$ HOX =  $\rho$ x where x is physical depth

 $d\tau = \kappa \rho dx$ 

ABROSS = Rosselan mean opacity

### *Requirement for chemical composition analyses: input line lists*

- o input atomic *and* molecular line lists
- $\circ$  at a fundamental level, abundance  $\propto$  Nf, where "N" is number density of absorbers and "f" is the oscillator strength
- $\circ$  if oscillator strength "f" is wrong, every other sophistication in your analysis is utterly useless
- o recent lab improvements make neglect of this issue a serious analysis flaw https://physics.osu.edu/research/atomic-molecular-and-optical-<br>https://physics.osu.edu/research/atomic-molecular-and-optical-



physics/agostini-dimauro-atomic-physics-research-group/lab

See DETAILS: slides 19–33

I am very interested (obsessed) with this issue

### A good summary site for lab atomic data



#### **Version 4**

Welcome to the NIST Atomic Spectra Database, NIST Standard Reference Database #78. The spectroscopic data may be selected and displayed according to wavelengths or energy levels by choosing one of the following options:



Spectral lines and associated energy levels displayed in wavelength order with all selected spectra intermixed or in multiplet order. Transition probabilities for the lines are also displayed where available.



Energy levels of a particular atom or ion displayed in order of energy above the ground state.

Warning: the transition probabilities at NIST are "curated"

this means that they have been often renormalized in individual NIST papers

#### **NIST ASD Team**

**Principal Developers (Currently Active):** 

Alexander Kramida, Yuri Ralchenko, and Joseph Reader

Data Compilers (Currently Active):

Alexander Kramida, Edward B. Saloman

**Database Developers (Currently Active):** 

Alexander Kramida, Yuri Ralchenko, and Karen Olsen

### NIST entries for Fe I near 4045Å: 6 lines



thoir octimated accuracios for lab values; he want of "C" and were  $\Lambda$   $\sim$ 

## But line lists for spectrum syntheses has 30 Fe I lines; they often come from semi-empirical line databases

#### **Robert L. Kurucz**

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This is a combined Web/outgoing-FTP site, KURUCZ.HARVARD.EDU or CFAKU5.CFA.HARVARD.EDU. It provides up-to-date public access to my data and programs. These are the same programs and files that I use in my research. Many bugs and problems have been corrected but there are still many more errors remaining to be found. Programs and data that I would not use myself because they are still under development are not on this computer. Many of the files are large and are also available on CDs or DVDs, and I am willing to write DVDs on demand. Some files taken from Kurucz CD-ROMs 1-26 are given for historical checks although many have been replaced by new versions. Binary versions will eventually be replaced by (much larger) ASCII versions. I am willing to rewrite them in ASCII on demand. Neither the programs nor data are "black boxes". You should not be using them if you do not have some understanding of the physics and of the programming in the source code.

#### the Kurucz line database has all sorts of transition data



There are more data than anonymous FTP can digest. Instead there is a user account with username GUEST and password CFAGUEST that can be accessed by FTP and TELNET. Simple OpenVMS commands like "TYPE file", "SEARCH file string", and "HELP" will work. The directories [NEWS], [VITABIB], [PAPERS], [ATOMS], [MOLECULES], [LINELISTS], [PROGRAMS], and [CDROMS] are on disk KU5E. [OPACITIES], [GRIDS], [SUN], and [STARS], are on KU5D, [TEMP] is on KU5C. and other directories and disks may be added. FTP does not execute the login so the logical names are not defined, but TELNET does. To go to a new directory "SET DEFAULT [name]". Case does not matter.

#### http://kurucz.harvard.edu/

## the dominant "compilation" transition data site

#### **Server: VALD Uppsala**

Version: 3740M

**Welcome to VALD3** 

Please enter your registered email address



VALD3



#### **About VALD**

etc.

**About VALD** 

**Documentation** 

**Documentation** 

**News** 

**VALD3 Mirror Servers** 

**VALD3 Mirror Uppsala** 

**VALD3 Mirror Montpellier** 

**VALD3 Mirror Moscow** 

**Contact / Registration** 

**Contact form** 

The Vienna Atomic Line Database (VALD) is a collection of atomic and molecular transition parameters of astronomical interest. VALD offers tools for selecting subsets of lines for typical astrophysical applications: line identification, preparing for spectroscopic observations, chemical composition and radial velocity measurements, model atmosphere calculations

The VALD Electronic Mail Service (VALD-EMS) is the main data transfer protocol for small data sets. For larger data extraction VALD users are advised to use the 'via ftp' option. This web portal is the main user interface to VALD VALD-EMS, It offers full functionality of the extraction tools and flexibility of data access. An alternative user interface and data transfer protocol are offered via the Virtual Atomic and Molecular Data Center (VAMDC). This option allows direct computer access to VALD and many other databases but it lacks some of the functionality that is present in the VALD extraction tools.

Below are the main ideas behind VALD concept that may help you using it in the most efficient way:

- . VALD extraction tools are constructed for intelligent selection of data relevant for specific astronomical problem.
- . Bulk data transfer via remote access is highly inefficient. For massive extraction (e.g. for computing opacity tables) you should consider hosting a mirror site. Contact the VALD administrator if you are interested.
- VALD is regularly updated with critically evaluated data sets. The VALD project team experts investigate the statistical properties of the data, extensively compare the results obtained with different data sources, and establish the quality rating for each new source which is a basis for data selection. This portal offers you a possibility to create and save an alternative ranking table that would also ensures reproducibility of the extraction.
- VALD data access is free but requires registration. Registration helps us rejecting spam, collecting statistics and informing you about updates. We do not share your registration information with anyone.

If you have any comments about VALD, or would like to register as a client, please contact us through our contact pages.

#### ❖ it is excellent!

- $\cdot$  the biggest concern is casual application by users
- ❖ VALD has all the necessary information to make critical assessment of line lists
- ❖ users need to take the time to understand from where line parameters have been taken
- ❖ users must assess the uniformity of transition data for individual species

## linemake: a simple curated line database

#### https://github.com/vmplacco/linemake



#### **Linemake Atomic and Molecular Line List** Generator

#### About

Linemake is an open-source atomic and molecular line list generator. Rather than a replacement for a number of well-established atomic and molecular spectral databases, linemake aims to be a lightweight, easy-to-use tool to generate formatted and curated lists suitable for spectral synthesis work. We stress that the users of should be in charge of all of their transition data, and should cite the appropriate sources in their published work, given below.

- + simple to download compile and execute
- + lab data sources are clearly labeled, and controlled in transparent ways
- + create synthetic spectrum lists or examine files for individual species
- +/– for syntheses, lines without trustworthy lab data are adopted from the Kurucz database
- output line lists are specifically for MOOG input (but one can modify the FORTRAN source code)
- almost always the choice is one lab source per species

Requirement for chemical composition analyses: "reliable" model atmosphere parameters Effective temperature  $T_{eff}$ : colors and/or spectral line data

- ➢ Colors: often B-V, V-I, V-K, J-K
	- ➢ Calibrated with "infrared flux method"
	- $\triangleright$  Gaia colors now contribute heavily to T<sub>eff</sub>
- $\triangleright$  spectral lines
	- $\triangleright$  "traditional" abundance vs excitation energy
		- ➢ requires well understood transition probabilities
		- $\triangleright$  done while deriving abundances in line analysis
	- ➢ becoming more common: line depth ratios (calibrated)
		- $\triangleright$  preselected and calibrated line depths sensitive to  $T_{\text{eff}}$
		- $\triangleright$  somewhat empirical approach

## T<sub>eff</sub> estimated from calibrated photometry



**works best with long color baseline extending into the near-IR sensitive to metallicity and dust obscuration effects**

## an empirical T<sub>eff</sub> method: absorption line depth ratios

Gray & Johanson 1991

![](_page_20_Figure_2.jpeg)

- this is Boltzmann/Saha at work as Teff decreases from spectral type goes from G0 V to K5 V
- V I 6251Å (E.P.=0.3eV) *grows* as V gets less ionized and as electrons go to lower excitation states
- Fe I 6252.6Å (E.P.=2.4eV) gets less ionized (more slowly that V!) but the higher excitation state loses electrons to lower states, so the absorption line depth changes more slowly
- NET: a big change in the line depth ratio  $-$  very sensitive T<sub>eff</sub> probe
- an empirical method; no detailed line parameters needed
- look for wavelength regions with "good" line pairs
- useful  $T_{\text{eff}}$  limits for a line pair:
	- too warm: one/both lines become too weak
	- too cool: both lines become hopelessly saturated
- between these limits good line ratios are very sensitive
- translation to  $T_{\text{eff}}$  is a question of calibration

![](_page_20_Figure_14.jpeg)

Biazzo 2007

## good line depth ratios can be found in any region

![](_page_21_Figure_1.jpeg)

Here is one example: IGRINS spectra of 2 red horizontal branch stars

Work out *without* calculations just why the spectra are similar & different

The listed model parameters,the line data, aided by Boltzmann & Saha, are all you need here

Afşar et al. 2023

In this paper identified 21 useful line ratios

Alas!! this method cannot really be used in the near-IR for gravity-sensitive line pairs … because there are very few ionized-species lines!

![](_page_21_Figure_8.jpeg)

![](_page_21_Figure_9.jpeg)

the star-to-star scatter in dominated by the LDR– $T_{eff}$ calibration relationship (usually linear or quadratic)

The big bonus: ability to estimate  $T_{\text{eff}}$  values in regions too dust-obscured to obtain optical spectra

Requirement for chemical composition analyses: "reliable" model atmosphere parameters Surface gravity log *g*: cluster, physical, and/or spectral line data Cluster:

![](_page_22_Figure_1.jpeg)

### to be more explicit on physical gravity

![](_page_23_Figure_1.jpeg)

### Requirement for chemical composition analyses: what we call "microturbulence"

#### sources of observed broadening of spectral lines:

- □ spectrograph instrumental broadening (you should know this)
- $\Box$  thermal but slowly changing (2kT/m)<sup>1/2</sup>
- □ microturbulence (affects total absorption of strong saturated lines)
- ❑ "damping": natural, Stark, van der Waals (affects strong lines)
- □ macroturbulence (large-scale motions; "no effect" on line strengths
- □ rotation (can't easily be disentangled from macroturbulence)
- ❑ magnetic fields
- $\Box$  starspots and other atmospheric complications

The microturbulent velocity is defined as the microscale non-thermal component of the gas velocity in the region of spectral line formation. Convection is the mechanism believed to be responsible for the observed turbulent velocity field, both in low mass stars and massive stars. https://en.wikipedia.org/wiki/Microturbulence

![](_page_24_Figure_11.jpeg)

![](_page_24_Figure_12.jpeg)

https://www.sciencedirect.com/topics/physicsand-astronomy/stellar-abundances

## $T_{\text{eff}}$ ,  $\log(g)$ ,  $v_{\text{micro}}$ , [Fe/H] metallicity, [X/Y] "all at once": iterative abundance calculations

![](_page_25_Figure_1.jpeg)

#### Some support for standard LTE stellar abundance analyses

![](_page_26_Figure_1.jpeg)

updates by, e.g. Asplund et al. 2009 do not change the basic agreement Sheden & Lawler 2005

### What about the critical CNO abundances?

- Carbon: CI, C<sub>2</sub> blue/yellow, CH blue, CN blue, red, near-IR, CO near-IR
	- lots of transitions; can you make them all agree?
- Nitrogen: CN from blue through near-IR
	- very dependent on first deriving C and O abundances
- Oxygen: O I, [O I], O-rich molecules in special cases
	- most abundances depend on ONLY the [O I] 6300.3Å line

#### When  $T_{\text{eff}}$  < 6000K, these are coupled and need molecular equilibrium calculations

![](_page_27_Figure_8.jpeg)

![](_page_27_Figure_9.jpeg)

## simplified molecular equilibrium: H-C-N-O

- $P(H) = p(H) + 2p(H2) + p(CH) + p(NH) + p(OH) + 2p(H2O) + ...$ **very coupled equartions**
- $P(C) = p(C) + p(CH) + 2p(C2) + p(CN) + p(CO) + p(CO2) + ...$
- $P(N) = p(N) + p(NH) + p(CN) + 2p(N2) + p(NO) + ...$
- $P(O) = p(O) + p(OH) + p(CO) + p(NO) + 2p(O2) + 2p(CO2) + ...$

But (happily!) the importance of each depends on abundance of the element(s) and the molecular dissociation energy

$$
\frac{p(AB)}{p(A)p(B)} = const \frac{\mathfrak{E}}{\mathfrak{E}M(AB)} \frac{\mathfrak{H}^{3/2}}{\mathfrak{E}} \frac{\mathfrak{E}}{\mathfrak{E}U(A)U(B)} \frac{\mathfrak{E}}{\mathfrak{E}} T^{-5/2} \exp_{\mathfrak{E}} \frac{\mathfrak{E}D_0}{kT \mathfrak{E}}
$$
  
\nP(H) = p(H) + 2p(H2) + ...  
\nP(C) = p(C) + p(CO) + ...  
\nP(N) = p(N) + 2p(N2) + ...  
\nP(D) = p(D) + p(CO) + ...  
\nP(D) = p(D) + p(D) + ...

**many codes quietly do this in the background…. but YOU must be aware**

### isotopic abundances: can be "easy" for molecular features

Carbon Magnesium

![](_page_29_Figure_3.jpeg)

can use  $\mathsf{C}_2$ , CH, CN, CO

Afşar et al 2018 McKenzie et al 2024 Sun: <sup>12</sup>C/<sup>13</sup>C ≃ 90 Sun: <sup>24</sup>Mg:<sup>25</sup>Mg:<sup>26</sup>Mg ≈ 79%:10%:11%

### much harder for atoms but not impossible

![](_page_30_Figure_1.jpeg)

![](_page_30_Figure_2.jpeg)

Sneden et al. 2014

#### See DETAILS: slides xx-xx for more good & bad examples

## final comments: pointing to where LTE simply fails

here is a plot of [Si/Fe] abundances in metal-poor stars using the dominant 3905Å Si I lines

Wait a minute: a temperaturedependent Si/Fe ratio simply cannot be right!

Given the claimed importance of Si in cosmic chemical evolution, we must do better

See DETAILS: slides 33–47

![](_page_31_Figure_5.jpeg)

![](_page_32_Figure_0.jpeg)

Here's the pragmatic problem: most published Cr and Mn abundances for metalpoor stars rely on the resonance lines

by factors of at least 2

![](_page_32_Figure_2.jpeg)

## This just scratches the surface!

Don't forget that abundances are supposed to tell us about stellar & Galactic chemical evolution

Thanks, and further contacts are welcome: chris@verdi.as.utexas.edu